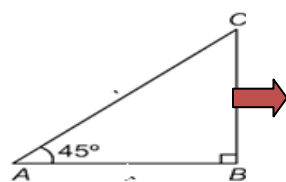


Trigonometric Ratios of 30°, 45°, 60°

Let's Recall:

- a) $\sin A = \frac{1}{\text{---}}$ d) $\cos A = \frac{1}{\text{---}}$
 b) $\tan A = \frac{1}{\text{---}}$ e) $\cot A = \frac{1}{\text{---}}$
 c) $\sec A = \frac{1}{\text{---}}$ f) $\operatorname{cosec} A = \frac{1}{\text{---}}$

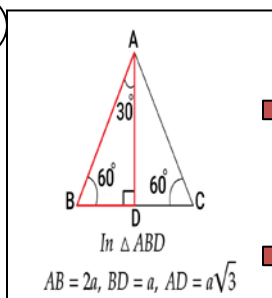


$AB = 1a, BC = 1a, AC = \sqrt{2}a$

$$\begin{aligned}\sin 45^\circ &= \frac{BC}{AC} = \frac{a}{a\sqrt{2}} = \frac{1}{\sqrt{2}} & \operatorname{cosec} 45^\circ &= \frac{1}{\sin 45^\circ} = \sqrt{2} \\ \cos 45^\circ &= \frac{AB}{AC} = \frac{a}{a\sqrt{2}} = \frac{1}{\sqrt{2}} & \sec 45^\circ &= \frac{1}{\cos 45^\circ} = \sqrt{2} \\ \tan 45^\circ &= \frac{BC}{AB} = \frac{a}{a} = 1 & \cot 45^\circ &= \frac{1}{\tan 45^\circ} = 1\end{aligned}$$

Can we find values for different trigonometric ratios?

Let's try.



$AB = 2a, BD = a, AD = a\sqrt{3}$

$$\begin{aligned}\sin 60^\circ &= \frac{AD}{AB} = \frac{\frac{\sqrt{3}}{2}a}{2a} = \frac{\sqrt{3}}{2} & \operatorname{cosec} 60^\circ &= \frac{1}{\sin 60^\circ} = \frac{2}{\sqrt{3}} \\ \cos 60^\circ &= \frac{BD}{AB} = \frac{\frac{a}{2}}{2a} = \frac{1}{2} & \sec 60^\circ &= \frac{1}{\cos 60^\circ} = 2 \\ \tan 60^\circ &= \frac{AD}{BD} = \frac{\frac{\sqrt{3}}{2}a}{\frac{a}{2}} = \sqrt{3} & \cot 60^\circ &= \frac{1}{\tan 60^\circ} = \frac{1}{\sqrt{3}}\end{aligned}$$

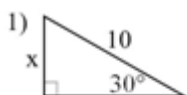
$$\begin{aligned}\sin 30^\circ &= \frac{BD}{AB} = \frac{\frac{a}{2}}{2a} = \frac{1}{2} & \operatorname{cosec} 30^\circ &= \frac{1}{\sin 30^\circ} = 2 \\ \cos 30^\circ &= \frac{AD}{AB} = \frac{\frac{\sqrt{3}}{2}a}{2a} = \frac{\sqrt{3}}{2} & \sec 30^\circ &= \frac{1}{\cos 30^\circ} = \frac{2}{\sqrt{3}} \\ \tan 30^\circ &= \frac{BD}{AD} = \frac{\frac{a}{2}}{\frac{\sqrt{3}}{2}a} = \frac{1}{\sqrt{3}} & \cot 30^\circ &= \frac{1}{\tan 30^\circ} = \sqrt{3}\end{aligned}$$

Example 1: Find values of given trigonometric ratios with the help of given table and write True or False:

Solution: $\sin 90^\circ = \cos 60^\circ$
 $\sin 90^\circ = 1, \cos 60^\circ = 1/2$
 as $1 \neq 1/2$, Therefore $\sin 90^\circ \neq \cos 60^\circ$
 Hence It's False.

Example 2: Find the value of x.

Solution:



$$\sin 30^\circ = \frac{x}{10}$$

$$\begin{aligned}\frac{1}{2} &= \frac{x}{10} \\ x &= 5\end{aligned}$$

Example 3: Solve:

Solution:

$$\begin{aligned}\sin 30^\circ \tan 45^\circ + \tan 30^\circ \sin 60^\circ &= \frac{1}{2}(1) + \frac{\sqrt{3}}{3}\left(\frac{\sqrt{3}}{2}\right) \\ &= \frac{1}{2} + \frac{3}{6} \\ &= \frac{1}{2} + \frac{1}{2} \\ &= 1 \\ \cos 30^\circ \sin 45^\circ + \sin 30^\circ \tan 60^\circ &= \frac{\sqrt{3}}{2}\left(\frac{\sqrt{2}}{2}\right) + \frac{1}{2}\left(\frac{\sqrt{3}}{3}\right) \\ &= \frac{\sqrt{6}}{4} + \frac{\sqrt{3}}{6} \\ &= \frac{\sqrt{6} \times 3 + \sqrt{3} \times 2}{4 \times 3 + 6 \times 2}\end{aligned}$$

Let's put values of all trigonometric ratios in table:

angle θ ratio	0°	30°	45°	60°	90°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	not defined
$\operatorname{cosec} \theta$	not defined	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1
$\sec \theta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	not defined
$\cot \theta$	not defined	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0

Now try these:

Let's learn a trick to remember values of trigonometric ratios:

	0°	30°	45°	60°	90°
$\sin \theta$	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	∞
$\cot \theta$	∞	$\sqrt{3}$	1	$\frac{1}{\sqrt{3}}$	0
$\sec \theta$	1	$\frac{2}{\sqrt{3}}$	$\sqrt{2}$	2	∞
$\operatorname{cosec} \theta$	∞	2	$\sqrt{2}$	$\frac{2}{\sqrt{3}}$	1

- Q1. Write True or False: a) $\sin 60^\circ = \cos 30^\circ$ b) $\sin 45^\circ = \cos 45^\circ$
 c) $\tan 60^\circ = \cot 60^\circ$ d) $\operatorname{cosec} 30^\circ = \cot 30^\circ$

Q2. In rt. $\triangle ABC$, right angled at B, $AB = 5\text{cm}$ and $\angle ACB = 30^\circ$. Determine the length of the sides BC and AC.

Q3. Find all the trigonometric ratios for the following triangle:

